

ANALYSES OF STREAM LINE AND TEMPERATURE FIELD OF LID DRIVEN CAVITY WITH A HEATED BARRIER

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ABSTRACT: In this investigation we focused on problem of combined convection fluid flow of Al_2O_3 - water in lid driven square cavity. The cavity containing a heated obstacle subjected to nanofluid while temperature and nanoparticles concentration dependent thermal conductivity and effective viscosity inside a square cavity. The governing equations have been calculated utilizing the FVM method while the SIMPLER algorithm is used to couple velocity and pressure fields.

KEYWORDS: Heat Transfer, Streamline, Convection, Nanofluid.

INTRODUCTION

Nanofluids are a suspension of nano-sized solid particles in a base fluid ethylene glycol, water or propylene glycol. The first to coin the "nanofluids" for these fluids with higher thermal properties was [Choi, \(1995\)](#). Existence of high thermal conductivity metallic nanoparticles in base fluid increases the thermal conductivity of such mixtures; hence conventional fluids have a rather low thermal conductivity with respect to nanofluids. So, different types of nanofluids are used to enhance the rate of heat transfer in many practical engineering applications ([Choi et al., \(2004\)](#); [Godson et al. \(2010\)](#) and [sarkar et al., \(2011\)](#)).

Many researchers have investigated on the thermophysical properties of nanofluids such as effective dynamic viscosity, thermal conductivity, thermal expansion coefficient and etc. ([Lee et al., \(1999\)](#); [Xie et al., \(2002\)](#); [Patel et al., \(2005\)](#) and [Chang et al., \(2005\)](#)). Moreover many theoretical, numerical and experimental studies on influence of existence of nanoparticle in convective heat transfer have been reported.

The first study concerning natural convection of a nanofluid confined in a differentially heated enclosure seems to be due to [Khanafar et al., \(2003\)](#). A comparative study of different models based on the thermophysical properties of copper-water nanofluid is developed and investigated. Their numerical results indicate that the suspended nanoparticles substantially increase the heat transfer rate

at any given Grashof number. A heat transfer correlation of the average Nusselt number for various Grashof numbers and volume fraction is proposed by the authors. The same problem was considered by [Lou and Tzeng, \(2006\)](#). The Khanafar and coworker's model was used to investigate the convective heat transfer enhancement in rectangular enclosures filled with an Al_2O_3 -water nanofluid. It was also reported that increasing the buoyancy parameter and volume fraction cause an increase in the average heat transfer coefficient. Natural convection heat transfer of nanofluids in a square cavity, heated isothermally from the vertical sides, has been investigated numerically by [Ho et al., \(2008\)](#) and [Santra et al., \(2008\)](#).

[Chen et al., \(2007\)](#) considered Darcy-Brinkman-Forchheimer extended model to examine free convection inside a porous cavity. This model has been initially introduced by [Brinkman, \(1947\)](#) in order to account for the transition from Darcy flow to highly viscous flow, in the limit of high permeability. Darcy-Forchheimer model is based on the effect of inertia and viscous forces in the porous media.

This model was used by [Poulikakos and Bejan, \(1985\)](#) and [Lauriat and Prasad, \(1989\)](#) in order to investigate the natural convection in a vertical enclosure filled with a porous medium. The extended Darcy-Forchheimer model was also used to describe resistance to flow through the porous baffles by [Miranda and Anand,](#)

(2004). Al-Amiri *et al.* (2008) investigated the wall heat conduction effect on the natural-convection heat transfer within a two-dimensional cavity, which is filled with a fluid-saturated porous medium and their study was based on Forchheimer - Brinkman-extended Darcy model.

Several investigates on mixed convection in single or double lid-driven enclosure flow and heat transfer including different cavity geometries and configurations, different base fluids and boundary condition have been reported. Effect of existence a obstacles within the cavity is one of the interesting investigations for researchers. Recently free convection fluid flow and heat transfer investigated numerically by Mahmoodi and Mazrouei, (2012). Their work was included of Cu-water nanofluid around the adiabatic square bodies at the center of a square cavity. They illustrated that for most Rayleigh numbers the Nusselt number increases with increase in the volume fraction of the nanoparticles. They also showed that at low Rayleigh numbers by increasing the size of the adiabatic square body, the rate of heat transfer decreases and opposite is true at high Rayleigh numbers. Mixed convection of Al₂O₃-water nanofluid in cavity with hot moving bottom wall and cold right, left, and top walls is investigated numerically by Mahmoodi, (2011). Also in valuable study, the effect of nanofluid variable properties on mixed convection in a rectangular cavity has been analyzed by Mazrouei Sebdani *et al.*, (2012).

MODELING AND GOVERNING EQUATIONS

Fig. 1 shows the physical model of the present study schematically. The system is considered to be unsteady, laminar, incompressible mixed convective flow and heat transfer in a two dimensional square cavity of length L filled with nanofluid.

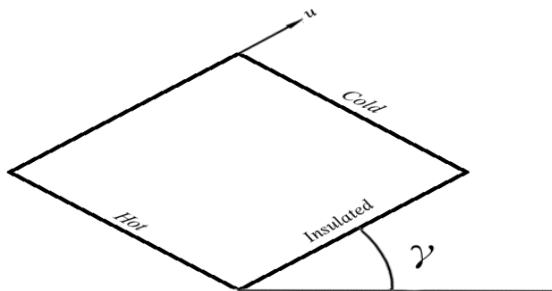


Figure 1: diagram of square inclined lid-driven cavity.

The cavity is filled with a suspension of Al₂O₃ nanoparticles in water that the nanoparticles and the base fluid are in thermal equilibrium and there is no slip between them.

The governing equations for a steady, two-dimensional laminar and incompressible flow are expressed as:

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0,$$

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = -\frac{1}{\rho_{nf}} \frac{\partial p}{\partial x} + \nu_{nf} \nabla^2 u, \tag{1}$$

$$u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = -\frac{1}{\rho_{nf}} \frac{\partial p}{\partial y} + \nu_{nf} \nabla^2 v + \frac{(\rho\beta)_{nf}}{\rho_{nf}} g \Delta T, \tag{2}$$

and

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \alpha_{nf} \nabla^2 T. \tag{3}$$

The dimensionless parameters may be presented as

$$X = \frac{x}{L}, Y = \frac{y}{L}, V = \frac{v}{u_0}, U = \frac{u}{u_0}$$

$$\Delta T = T_h - T_c, \theta = \frac{T - T_c}{\Delta T}, P = \frac{p}{\rho_{nf} u_0^2}. \tag{4}$$

Hence,

$$Re = \frac{\rho_f u_0 L}{\mu_f}, Ri = \frac{Ra}{Pr \cdot Re^2}, Ra = \frac{g \beta_f \Delta T L^3}{\nu_f \alpha_f}, Pr = \frac{\nu_f}{\alpha_f}. \tag{5}$$

The dimensionless form of the above governing equations (1) to (4) become

$$\frac{\partial U}{\partial X} + \frac{\partial V}{\partial Y} = 0 \tag{6}$$

$$U \frac{\partial U}{\partial X} + V \frac{\partial U}{\partial Y} = -\frac{\partial P}{\partial X} + \frac{\nu_{nf}}{\nu_f} \frac{1}{Re} \nabla^2 U \tag{7}$$

$$U \frac{\partial V}{\partial X} + V \frac{\partial V}{\partial Y} = -\frac{\partial P}{\partial Y} + \frac{\nu_{nf}}{\nu_f} \frac{1}{Re} \nabla^2 V + \frac{Ri}{Pr} \frac{\beta_{nf}}{\beta_f} \Delta \theta \tag{8}$$

and

$$U \frac{\partial \theta}{\partial X} + V \frac{\partial \theta}{\partial Y} = \frac{\alpha_{nf}}{\alpha_f} \nabla^2 \theta \tag{9}$$

2.1. Thermal Diffusivity And Effective Density

Thermal diffusivity and effective density of the nanofluid are

$$\alpha_{nf} = \frac{k_{nf}}{(\rho c_p)_{nf}} \tag{10}$$

$$\rho_{nf} = \varphi\rho_s + (1 - \varphi)\rho_f \quad (12)$$

2.2. Heat Capacity And Thermal Expansion Coefficient

Heat capacity and thermal expansion coefficient of the nanofluid are therefore

$$(\rho c_p)_{nf} = \varphi(\rho c_p)_s + (1 - \varphi)(\rho c_p)_f \quad (13)$$

$$(\rho\beta)_{nf} = \varphi(\rho\beta)_s + (1 - \varphi)(\rho\beta)_f$$

2.3. Viscosity

The effective viscosity of nanofluid was calculated by:

$$\mu_{eff} = \mu_f (1 + 2.5\varphi) \left[1 + \eta \left(\frac{d_p}{L} \right)^{-2\varepsilon} \varphi^{2/3} (\varepsilon + 1) \right] \quad (14)$$

This well-validated model is presented by Jang and coworkers. For a fluid containing a dilute suspension of small rigid spherical particles and it accounts for the slip mechanism in nanofluids. The empirical constant ε and η are -0.25 and 280 for Al_2O_3 ; respectively. It is worth mentioning that the viscosity of the base fluid (water) is considered to vary with temperature and the flowing equation is used to evaluate the viscosity of water,

$$\mu_{w,p} = (1.2723 \times T_c^{-3} - 8.736 \times T_c^{-4} + 33.708 \times T_c^{-5} - 246.6 \times T_c^{-6} + 518.78 \times T_c^{-7} + 1153.9) \times 10^6 \quad (15)$$

Where, $T_{rc} = \text{Log}(T - 273)$.

2.4. Dimensionless Stagnant Thermal Conductivity

The effective thermal conductivity of the nanoparticles in the liquid as stationary is calculated by the Hamilton and crosser (H-C model)(1962), which is:

$$\frac{k_{stationary}}{k_f} = \frac{k_s + 2k_f - 2\varphi(k_f - k_s)}{k_s + 2k_f + \varphi(k_f - k_s)} \quad (16)$$

2.5. Total Dimensionless Thermal Conductivity Of Nanofluids

$$\frac{k_{nf}}{k_f} = \frac{k_{stationary}}{k_f} + \frac{k_c}{k_f} = \frac{k_s + 2k_f - 2\varphi(k_f - k_s)}{k_s + 2k_f + \varphi(k_f - k_s)} + c \frac{Nu_p d_f (2 - D_f) D_f \left[\left(\frac{d_{max}}{d_{min}} \right)^{1-2D_f} - 1 \right]^2}{Pr(1 - D_f)^2 \left(\frac{d_{max}}{d_{min}} \right)^{2-2D_f} - 1} d_f^*$$

This model was proposed by Xu and coworkers in which it has been chosen in this study to describe the thermal conductivity of nanofluids. c is an empirical constant (e.g. $c = 85$ for the deionized water and $c = 280$ for ethylene glycol) but independent of the type of nanoparticles. Nu_p is the Nusselt number for liquid flowing around a spherical particle and equal to two for

a single particle in this work. The fluid molecular diameter $d_f = 4.5 \times 10^{-10}$ (m) for water in present study. The fractal dimension D_f is determined by:

$$D_f = 2 - \frac{\ln \varphi}{\ln \left(\frac{d_{p,min}}{d_{p,max}} \right)}$$

Where, $d_{p,max}$ and $d_{p,min}$ are the maximum and minimum diameters of nanoparticles, respectively. Ratio of minimum to maximum nanoparticles $d_{p,min}/d_{p,max}$ is R.

$$d_{p,max} = d_p \cdot \frac{D_f - 1}{D_f} \left(\frac{d_{p,min}}{d_{p,max}} \right)^{-1}$$

$$d_{p,min} = d_p \cdot \frac{D_f - 1}{D_f}$$

NUMERICAL APPROACH

Continuity, momentum and energy equations are discretized using the finite volume method and with staggered grid system. The convection terms is approximated by a blend of central difference scheme and upwind scheme (hybrid-scheme) which is conducive to a stable solution. Besides, a second-order central differencing scheme is served to the diffusion terms. The algebraic system arising from numerical discretization is computed using Tridiagonal Matrix Algorithm (TDMA) To verify grid independence, numerical procedure was examined for nine different mesh sizes, namely; 21×21 , 31×31 , 41×41 , 51×51 , 61×61 , 71×71 , 81×81 , 91×91 and 101×101 . Average Nu at $Re=10$, and $\varphi=0.06$ is attained for each grid size as shown in Fig 2.

As can be observed, 91×91 uniform grid size yields the required accuracy and was hence applied for all simulation exercises in this work as presented in the following section.

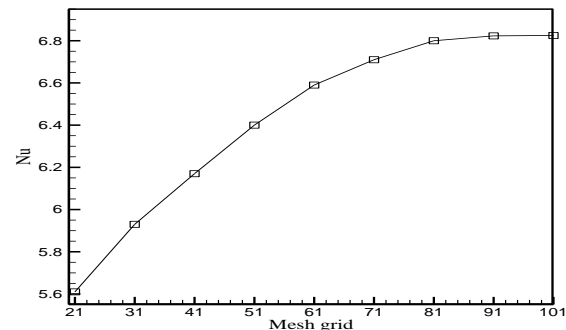


Figure 2: grid study

RESULTS AND DISCUSSION

Fig. 3 exhibits streamlines and isotherms in different angles of cavity positioned in $Re=100$, $\varphi=0.05$ and $h=0.1L$. Flow pattern in horizontal

position of cavity shows formation of a primary clockwise cell which has almost occupied all the cavity space. As the cavity inclination is upraised to 30° , buoyancy and shear forces lose their perfect co-directionality and a change thus happens in flow pattern in the cavity. In such state, two small vortexes are composed resulted from the force of upper section movement lid and near the lid itself while the intensity of the main cell is a little reduced.

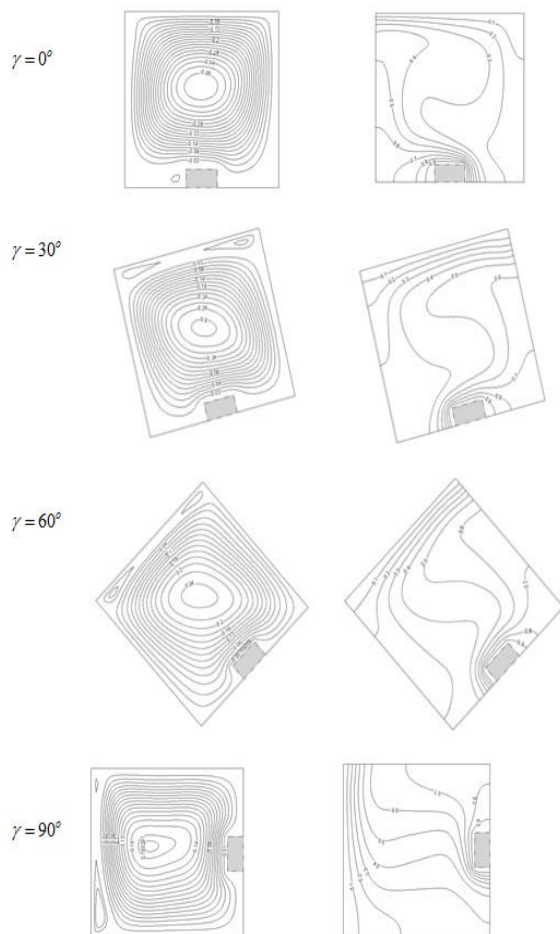


Figure 3: streamlines and isotherms in different angles of cavity positioned in $Re=100$, $T=300$.

As a result of the dominance of natural convection over forced convection in the Richardson range studied in this figure, the central cell resulted by buoyancy force is in all positions stronger than upper vortexes caused by shear force from upper lid. Isotherm lines show more intensity at areas close to hot walls.

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